

Semi-Federated Scheduling of Mixed-Criticality System for Sporadic DAG Tasks

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Outline

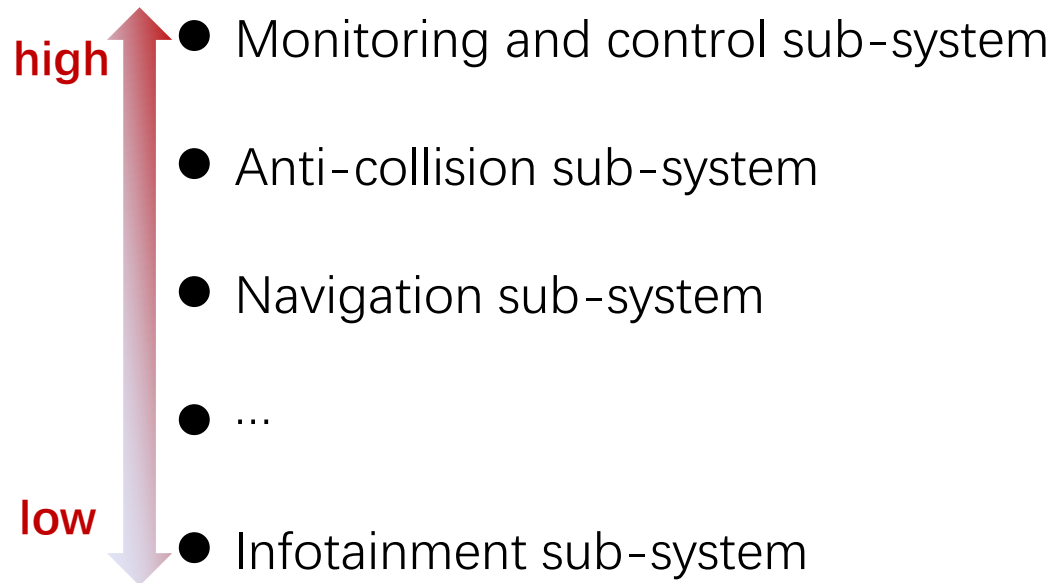
- Background & Contributions
- Preliminaries
- Semi-Federated Mixed-Criticality Algorithm
- Evaluation

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Mixed-Criticality Systems

Sub-systems with different criticality levels (e.g. avionics):



Mixed-Criticality Systems

Characteristics :

- More complex functions of system
- No reduction in system security requirements

Challenges:

- Multicore: no enough analytical techniques
- Task parallelization: dependencies and competitions among tasks

How to assign computation resources to parallel tasks on a multicore platform while guaranteeing security ?

Our work

Propose a semi-federated mixed-criticality scheduling algorithm

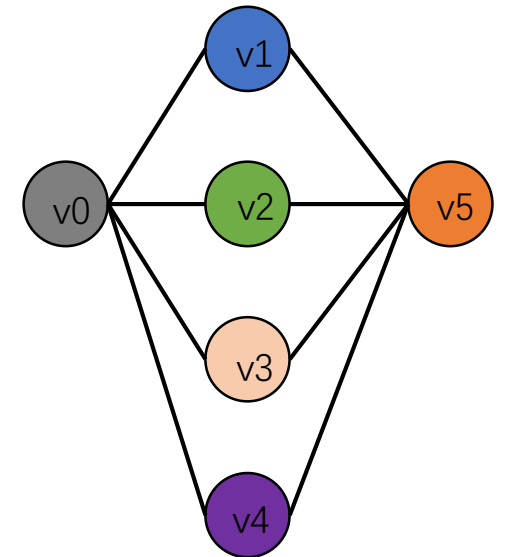
- Propose a mapping algorithm: from mixed-criticality tasks to a middleware layer (mixed-criticality container tasks)
- Prove the schedulability of our proposed algorithm

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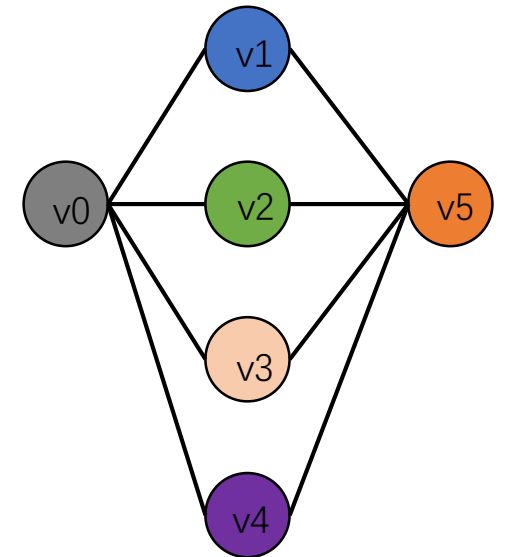
Mixed-Criticality Task Model

- Implicit-deadline sporadic parallel
- Each task is denoted by a directed acyclic graph
 - ✓ Vertices: sequential subtasks
 - ✓ Edges: dependencies
- Two types: low-criticality and high-criticality



Mixed-Criticality Task Model

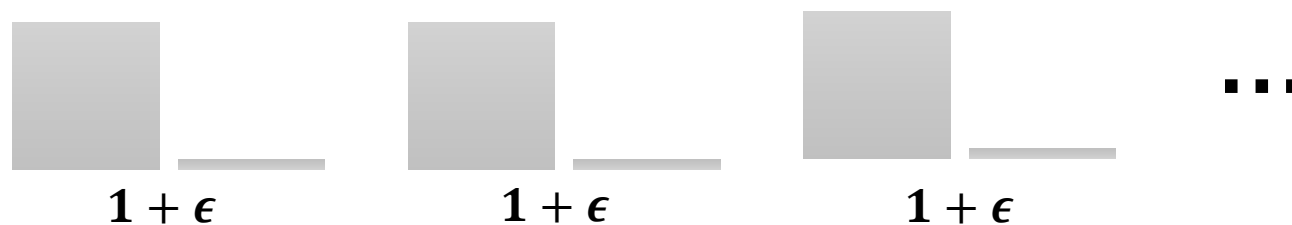
- **WCET** of a vertex (subtask): c^N and c^O
- **WCET** of a task: C^N and C^O
- **The longest chain** of a task: L^N and L^O
- **Deadline** of a task: D
- **Virtual deadline** of a task: D'
- **Task utilization**: $u^N = \frac{C^N}{D'}$ $u^O = \frac{C^O}{D - D'}$



Existing work: Federated Mixed-Criticality Scheduling

- Task types: LH, HVH, HMH
- System states: normal state and critical state
- Assigning strategy: independently usable cores to each task in the normal and critical states.

- **In the worst case, half of the resources are wasted**



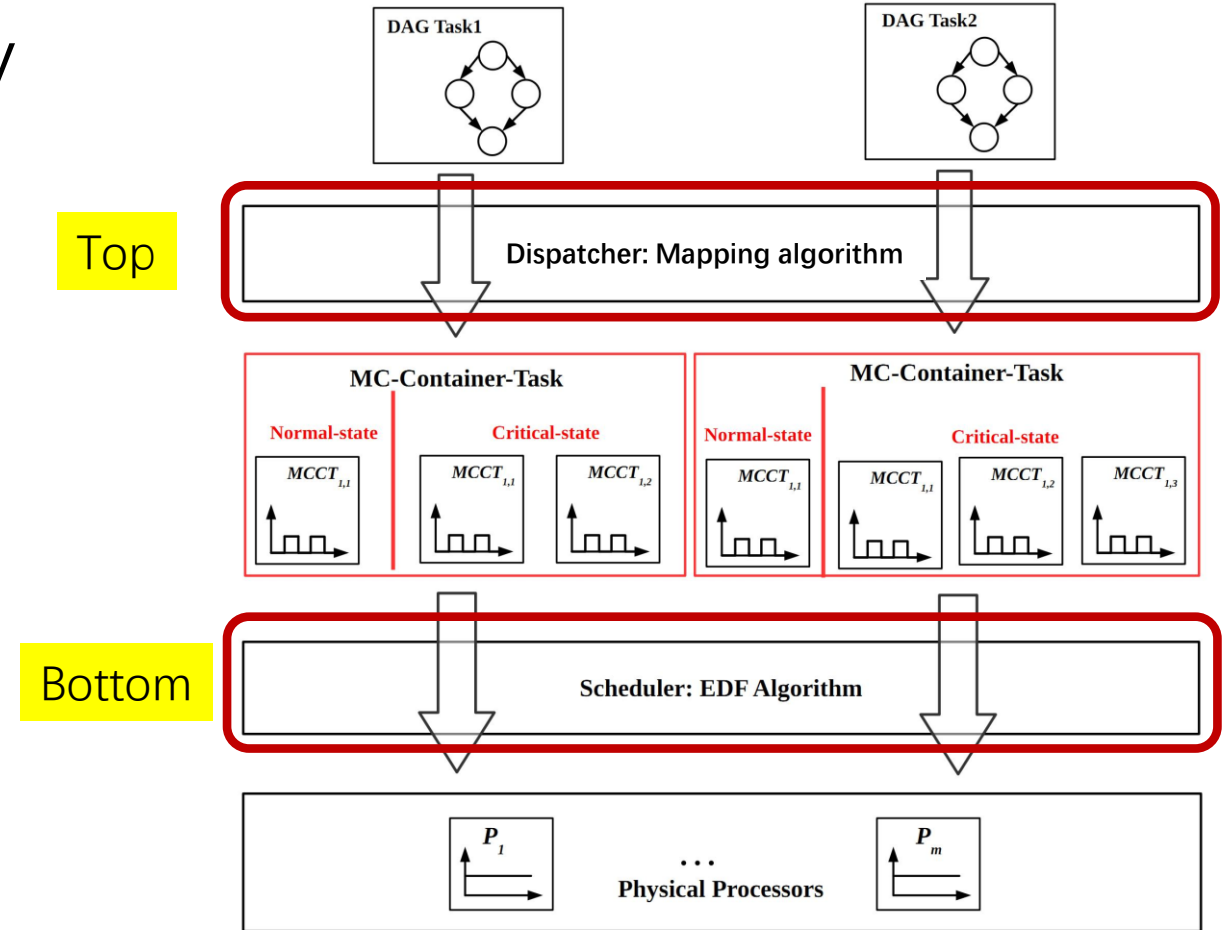
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Architecture of Our Algorithm

Semi-Federated Mixed-Criticality Algorithm:

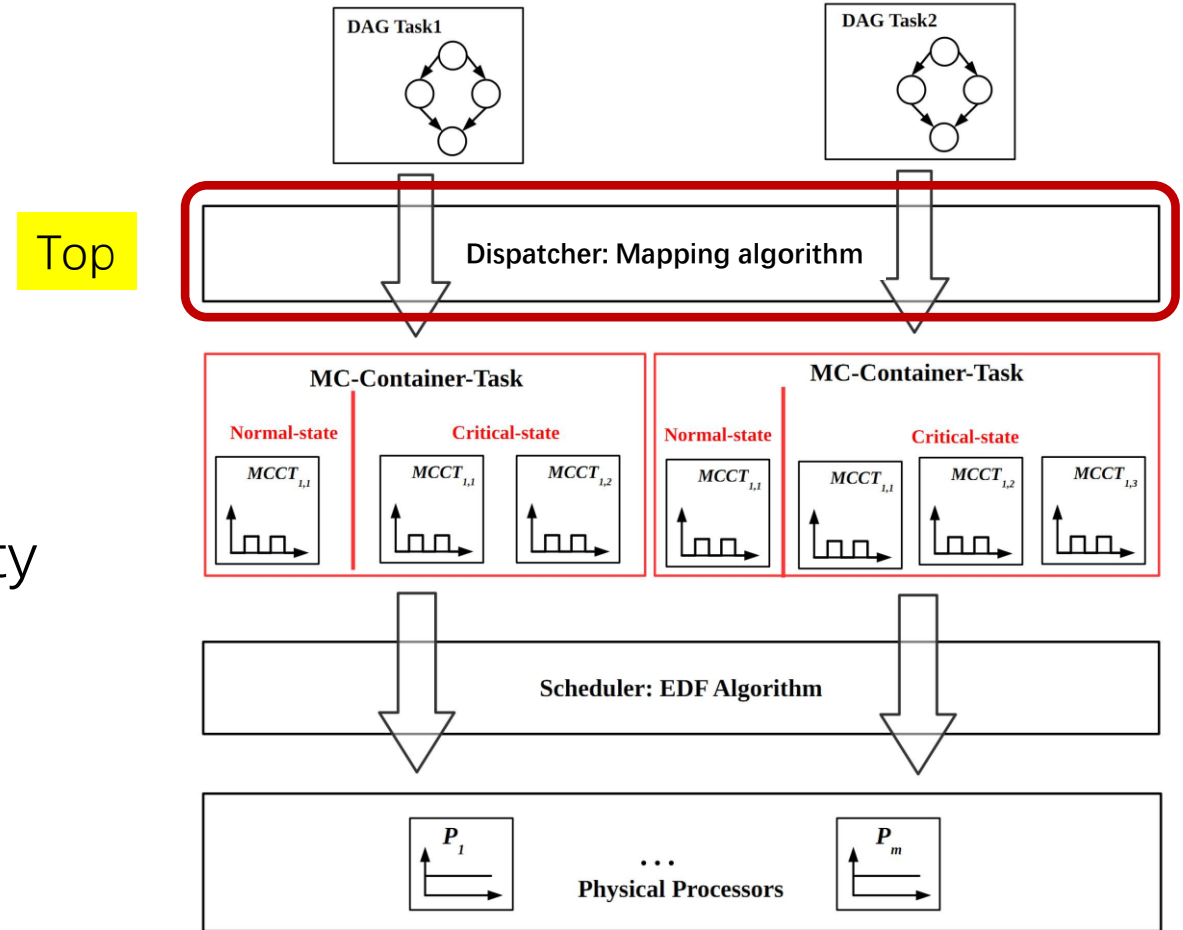
- Two-level hierarchical scheduling framework



Architecture of Our Algorithm

Semi-Federated Mixed-Criticality Algorithm:

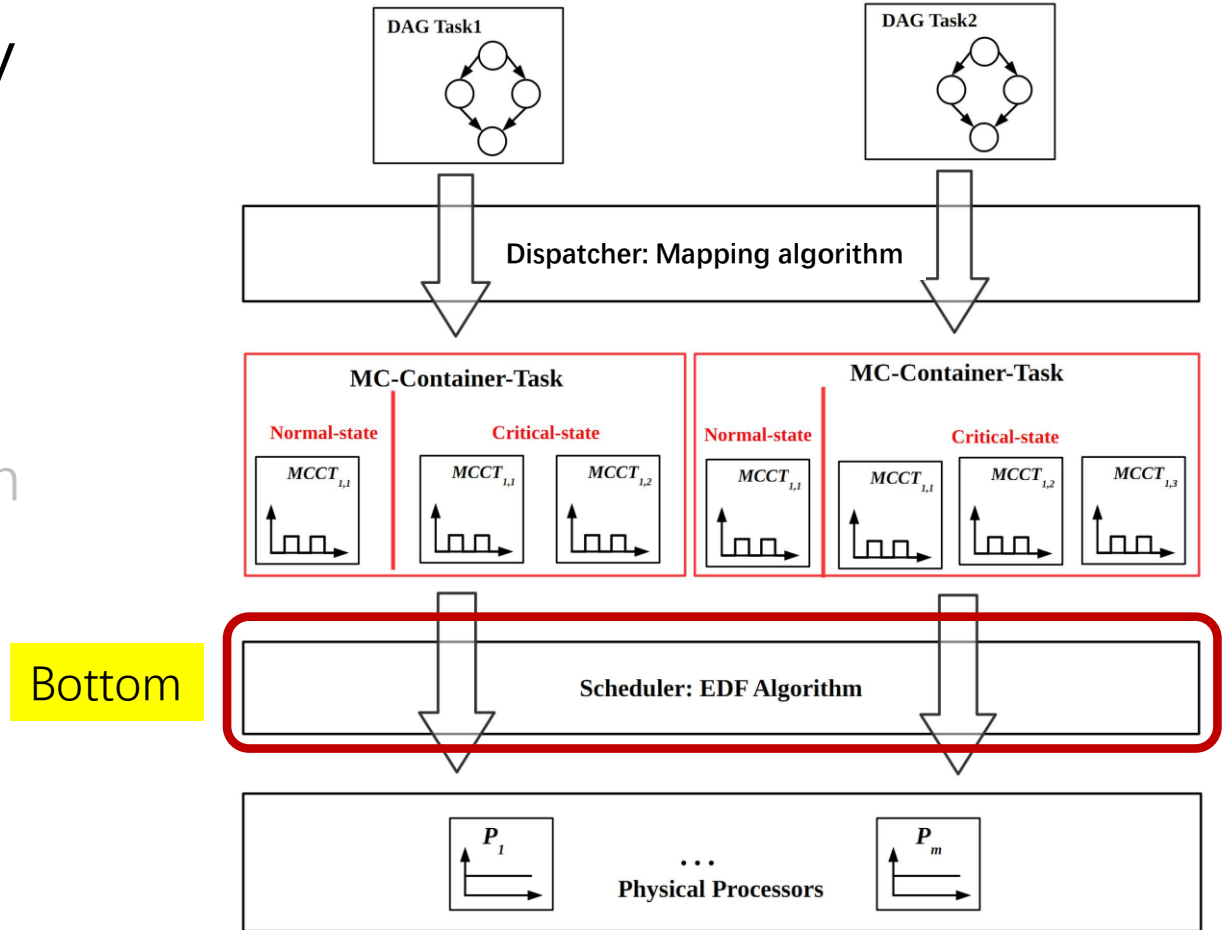
- Two-level hierarchical scheduling framework
- **Top-level** calculates the mapping from mixed-criticality tasks to mixed-criticality container-tasks.



Architecture of Our Algorithm

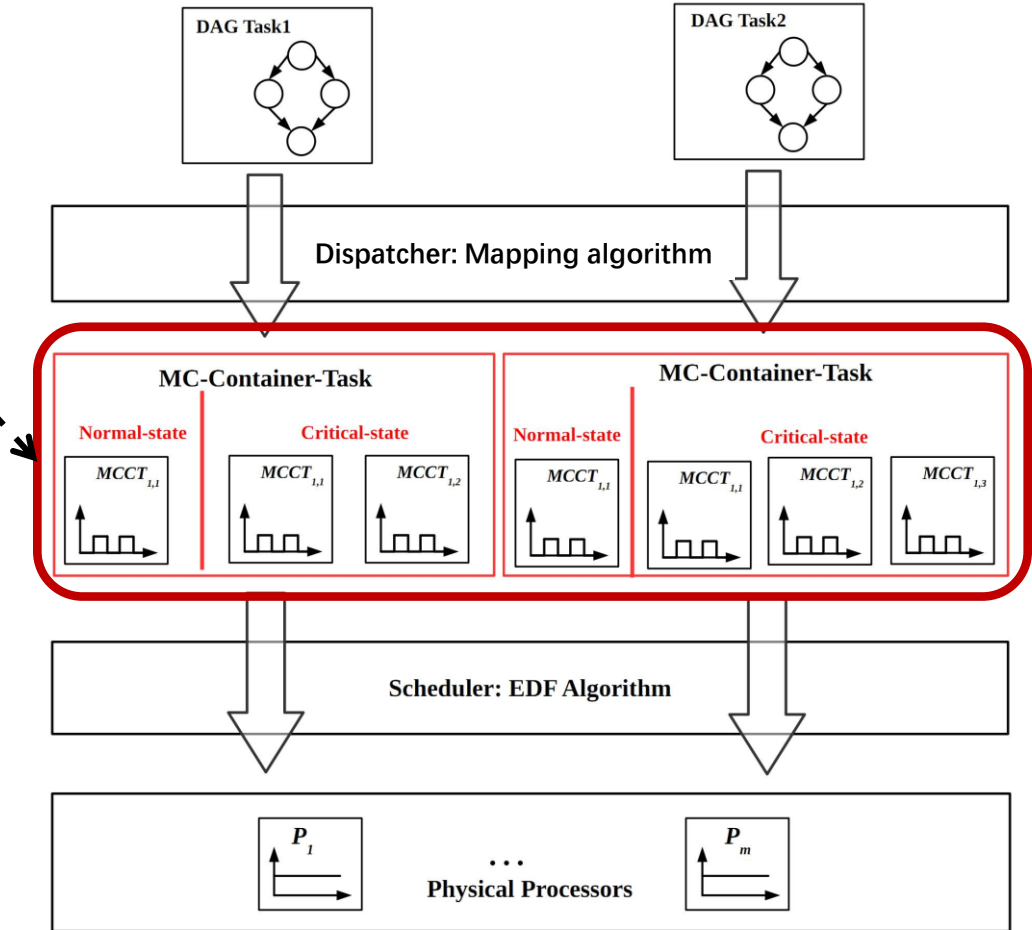
Semi-Federated Mixed-Criticality Algorithm:

- Two-level hierarchical scheduling framework
- Top-level calculates the mapping from mixed-criticality tasks to mixed-criticality container-tasks.
- **Bottom-level** schedules mixed-criticality container-tasks on physical processors.



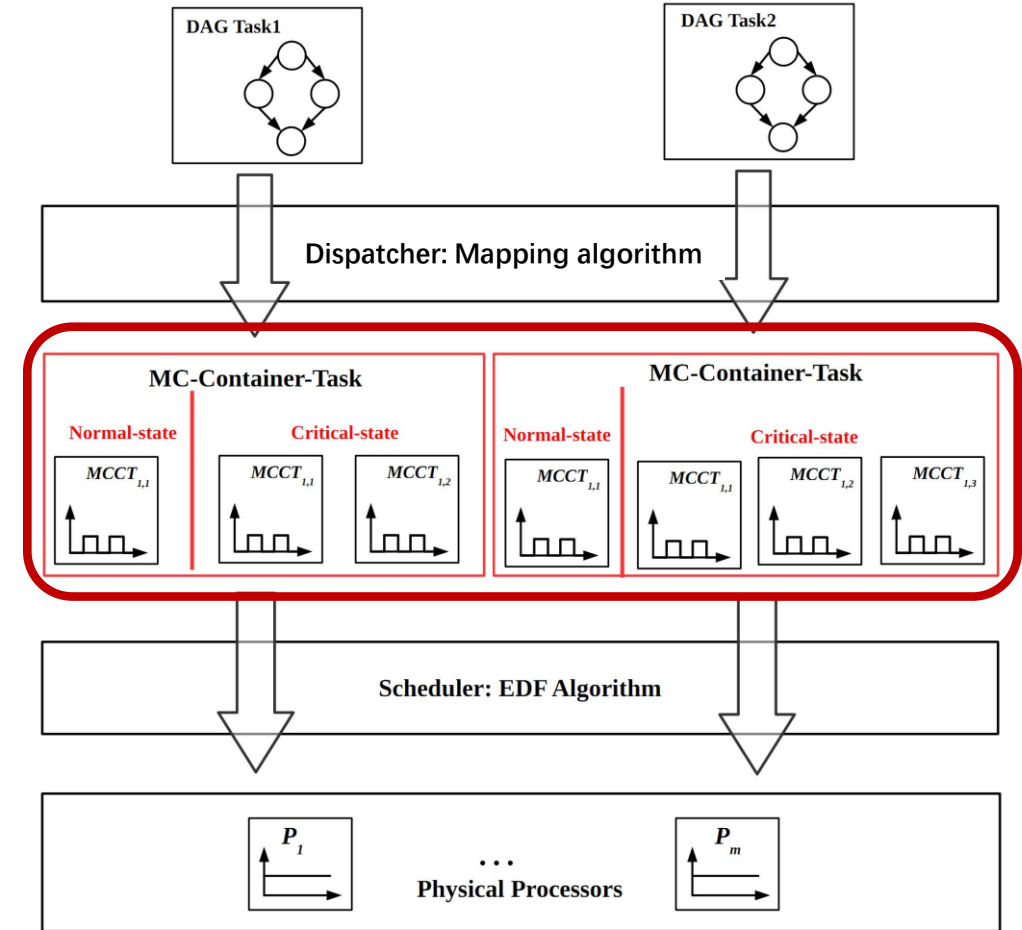
Mixed-Criticality Container Task

- Processor resources interface



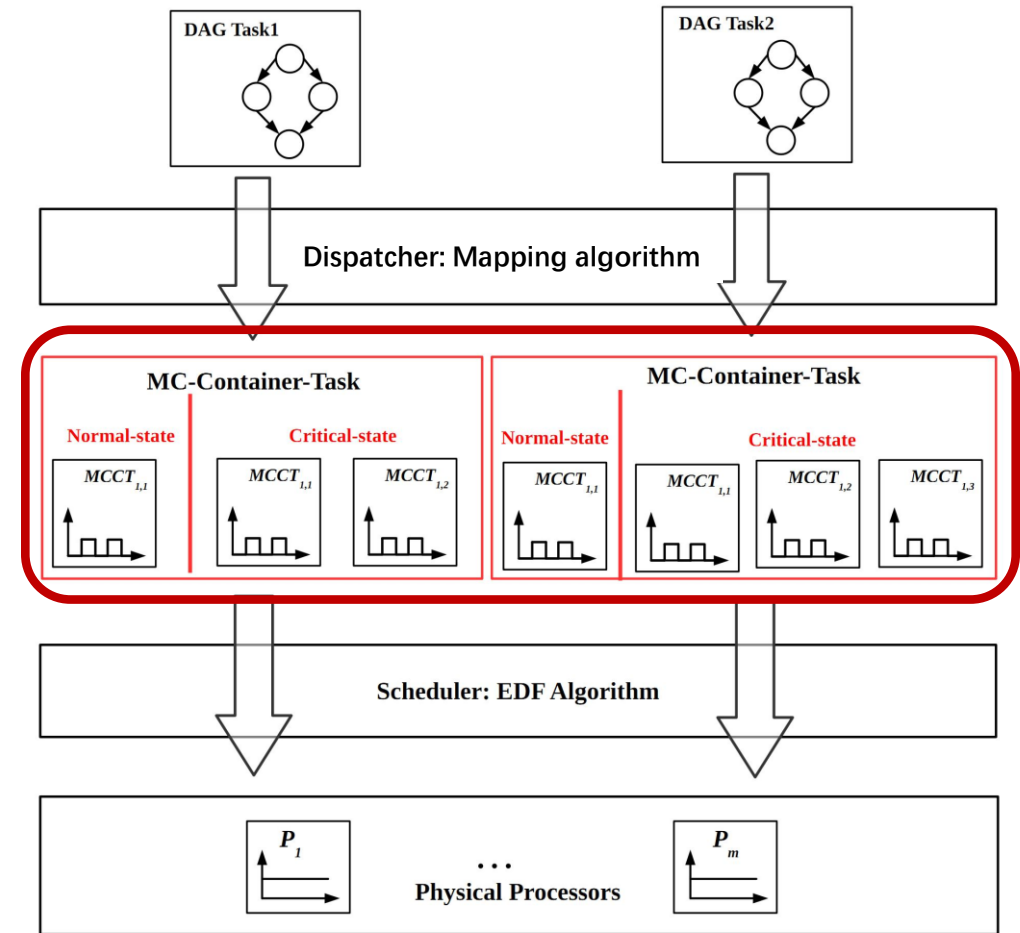
Mixed-Criticality Container Task

- Processor resources interface
- Calculate number of mixed-criticality container tasks in both normal states and critical states



Mixed-Criticality Container Task

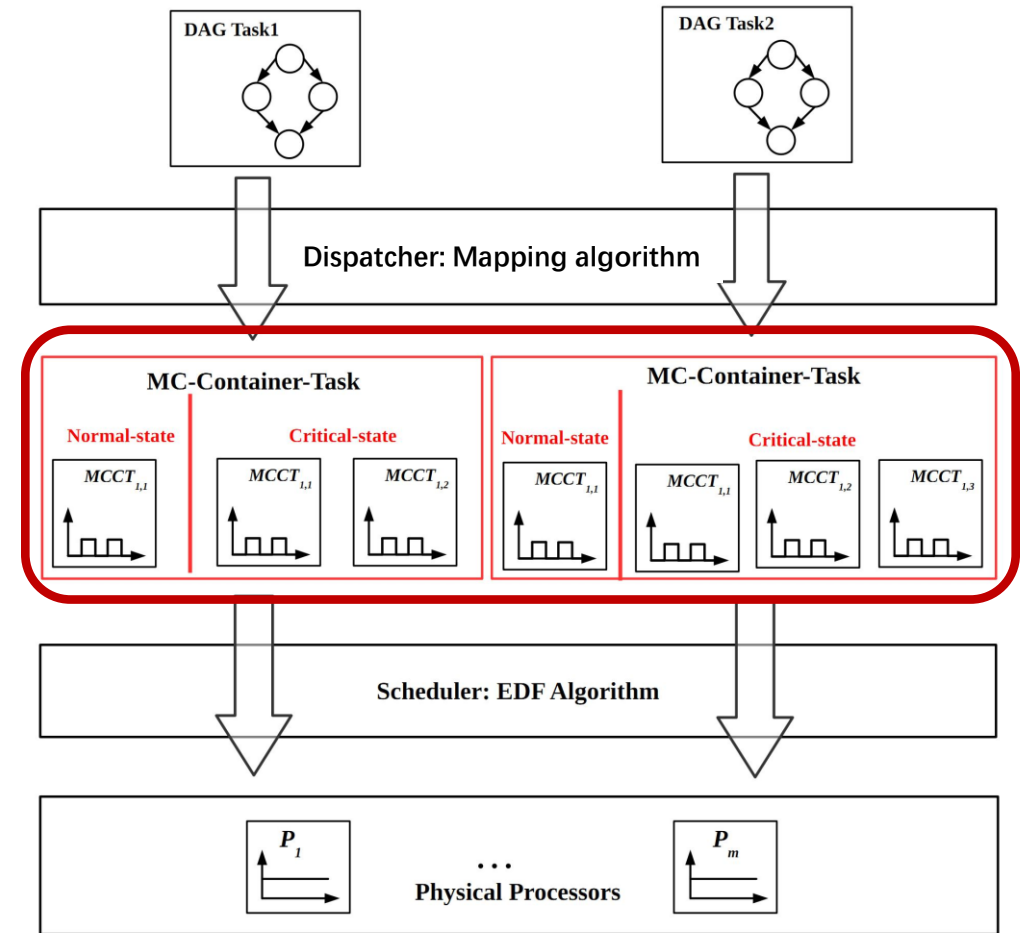
- Processor resources interface
- Semi-federated:
Mixed-criticality container tasks provide virtual resources, so the number of mixed-criticality task can be decimal, avoiding resource waste



Mixed-Criticality Container Task

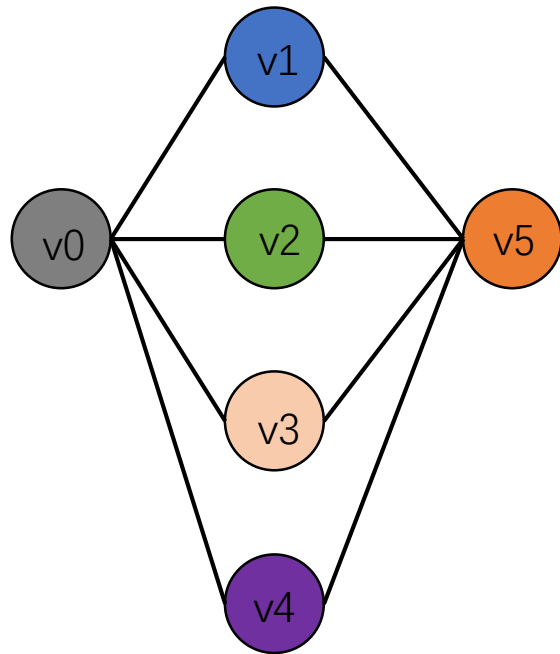
- Processor resources interface
- If the WCET of a task equals c when it executes on a unit speed processor, then its WCET on a container-task with speed σ is:

$$t = \frac{c}{\sigma}$$



Mapping Algorithm

A mixed-criticality task



$$c_{v0}^N = 1 \quad c_{v0}^O = 2,$$

$$c_{v2}^N = 1 \quad c_{v2}^O = 3,$$

$$c_{v4}^N = 1 \quad c_{v4}^O = 3,$$

$$D = 13, \quad D' = 5$$

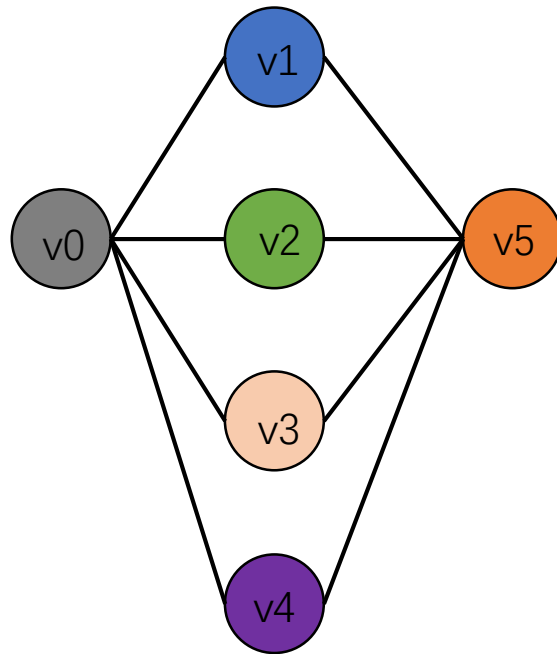
$$c_{v1}^N = 1 \quad c_{v1}^O = 3$$

$$c_{v3}^N = 1 \quad c_{v3}^O = 3$$

$$c_{v5}^N = 1 \quad c_{v5}^O = 2$$

Mapping Algorithm

A mixed-criticality task



$$c_{v0}^N = 1 \quad c_{v0}^O = 2, \quad c_{v1}^N = 1 \quad c_{v1}^O = 3$$

$$c_{v2}^N = 1 \quad c_{v2}^O = 3, \quad c_{v3}^N = 1 \quad c_{v3}^O = 3$$

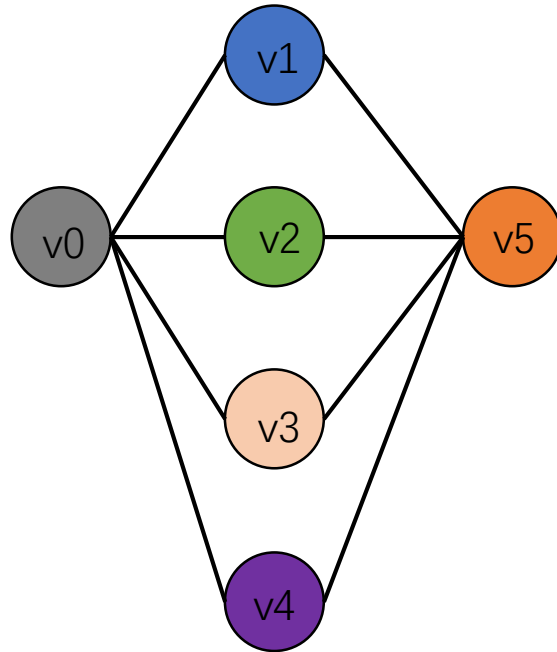
$$c_{v4}^N = 1 \quad c_{v4}^O = 3, \quad c_{v5}^N = 1 \quad c_{v5}^O = 2$$

$$D = 13, \quad D' = 5$$

$$C^N = 6, \quad C^O = 16, \quad L^N = 3, \quad L^O = 7$$

Mapping Algorithm

A mixed-criticality task



$$c_{v0}^N = 1 \quad c_{v0}^O = 2, \quad c_{v1}^N = 1 \quad c_{v1}^O = 3$$

$$c_{v2}^N = 1 \quad c_{v2}^O = 3, \quad c_{v3}^N = 1 \quad c_{v3}^O = 3$$

$$c_{v4}^N = 1 \quad c_{v4}^O = 3, \quad c_{v5}^N = 1 \quad c_{v5}^O = 2$$

$$D = 13, \quad D' = 5$$

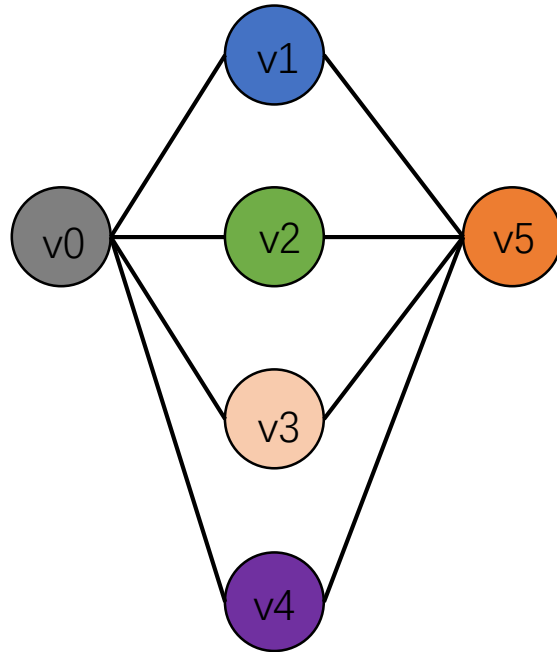
$$C^N = 6, \quad C^O = 16, \quad L^N = 3, \quad L^O = 7$$

$$u^N = \frac{C^N}{D'} = \frac{6}{5} > 1$$

Mapping Algorithm

A mixed-criticality task

- **Calculating the mapping**



$$C^N = 6, C^O = 16, L^N = 3, L^O = 7, D = 13, D' = 5$$

Using our mapping equation:

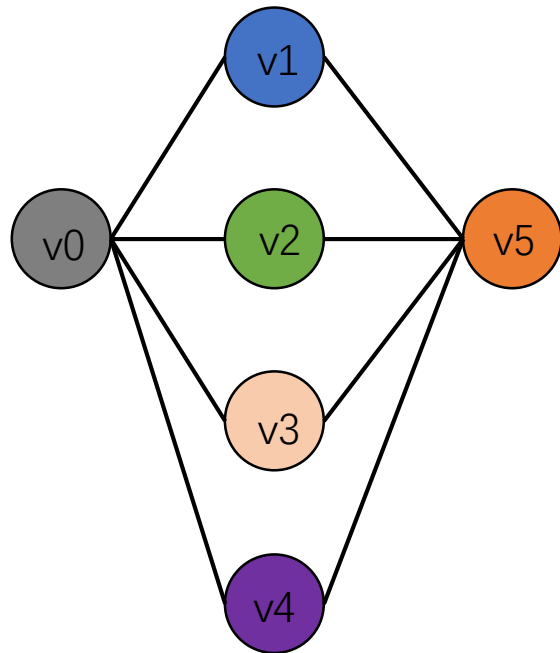
$$s_i^N = \begin{cases} u_i^N & \text{when } u_i^N < 1 \\ \frac{C_i^N - L_i^N}{D_i' - L_i^N} & \text{when } u_i^N \geq 1 \end{cases}$$

$$s_i^O = \begin{cases} 0 & \text{if task is LO} \\ \frac{C_i^O - s_i^N D_i' - L_i^O}{D_i - D_i' - L_i^O} & \text{if task is HI} \end{cases}$$

Mapping Algorithm

A mixed-criticality task

- Calculating the mapping



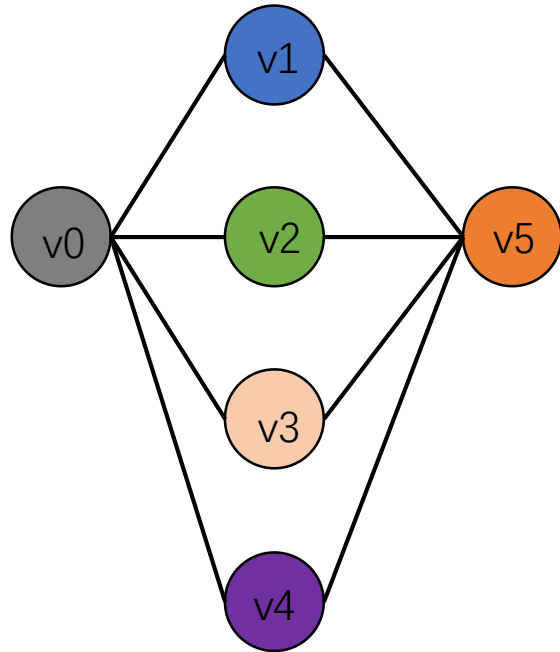
$$C^N = 6, C^O = 16, L^N = 3, L^O = 7, D = 13, D' = 5$$

$$S^N = \frac{C^N - L^N}{D' - L^N} = \frac{6 - 3}{5 - 3} = \mathbf{1.5}$$

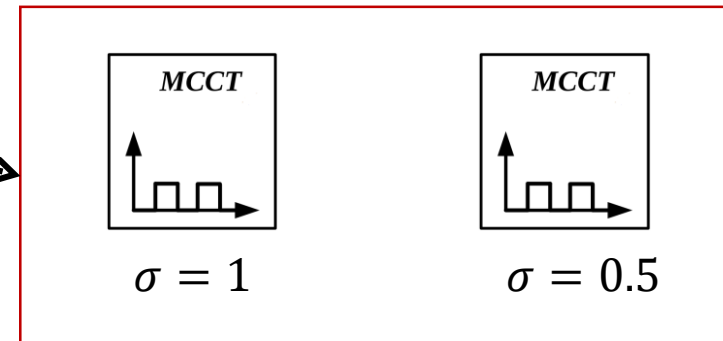
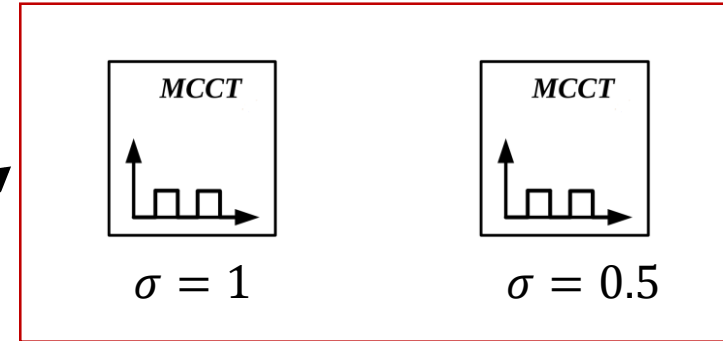
$$S^O = \frac{C^O - S^N D' - L^O}{D - D' - L^O} = \frac{16 - 1.5 * 5 - 7}{13 - 5 - 7} = \mathbf{1.5}$$

Mapping Algorithm

A mixed-criticality task



Mapping



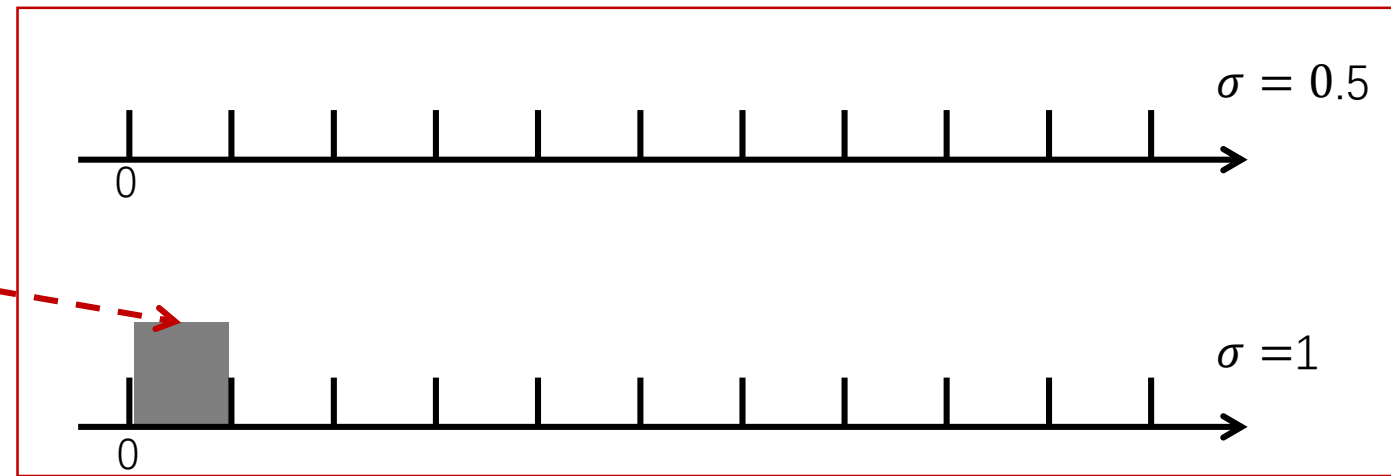
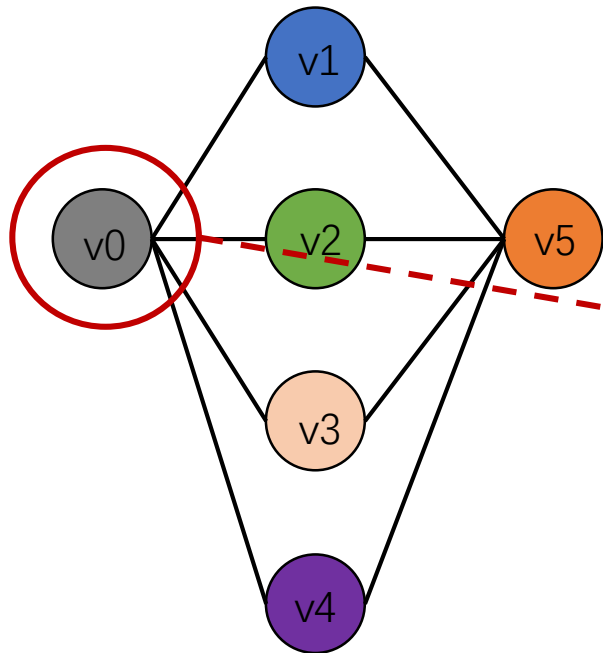
Runtime of a Mixed-Criticality Task

- Mixed-Criticality tasks are encapsulated into mixed-criticality container-tasks
- Scheduling these mixed-criticality container-tasks to physical processors with a partitioned or global algorithm

Runtime of a Mixed-Criticality Task

$$\begin{aligned}c_{v0}^N = 1 \quad c_{v0}^O = 2, & \quad c_{v1}^N = 1 \quad c_{v1}^O = 3 \\c_{v2}^N = 1 \quad c_{v2}^O = 3, & \quad c_{v3}^N = 1 \quad c_{v3}^O = 3 \\c_{v4}^N = 1 \quad c_{v4}^O = 3, & \quad c_{v5}^N = 1 \quad c_{v5}^O = 2\end{aligned}$$

- Mixed-Criticality tasks are encapsulated into mixed-criticality container-tasks
 - Encapsulating the vertex v_0

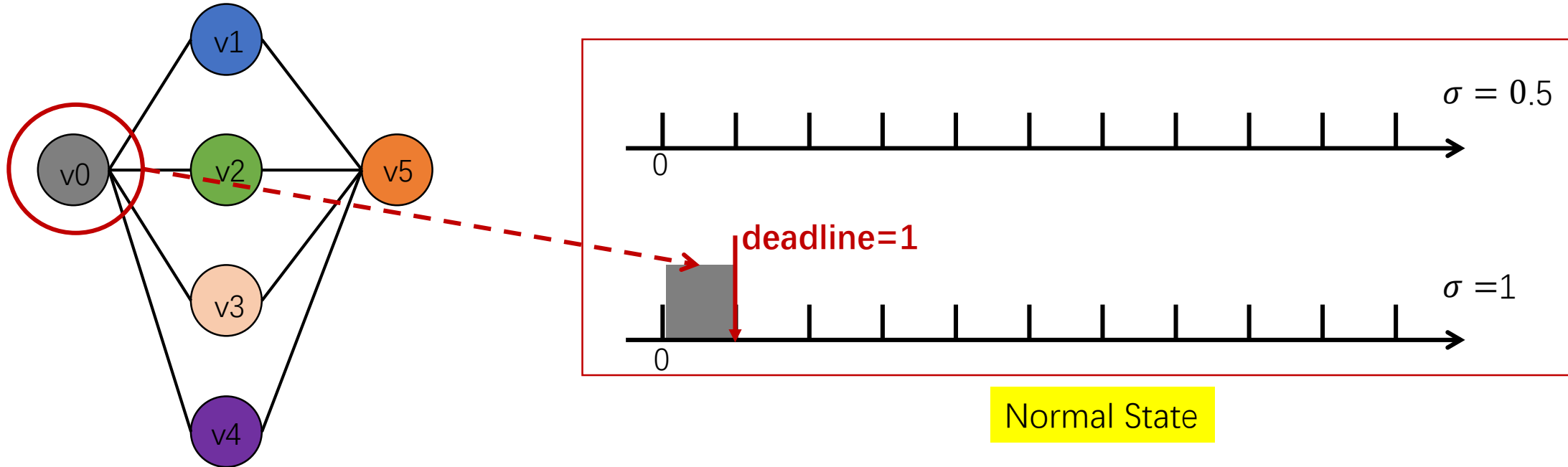


Normal State

Runtime of a Mixed-Criticality Task

$$\begin{aligned}c_{v0}^N = 1 \quad c_{v0}^O = 2, & \quad c_{v1}^N = 1 \quad c_{v1}^O = 3 \\c_{v2}^N = 1 \quad c_{v2}^O = 3, & \quad c_{v3}^N = 1 \quad c_{v3}^O = 3 \\c_{v4}^N = 1 \quad c_{v4}^O = 3, & \quad c_{v5}^N = 1 \quad c_{v5}^O = 2\end{aligned}$$

- Mixed-Criticality tasks are encapsulated into mixed-criticality container-tasks
 - **Setting the deadline of the mixed-criticality container-task**

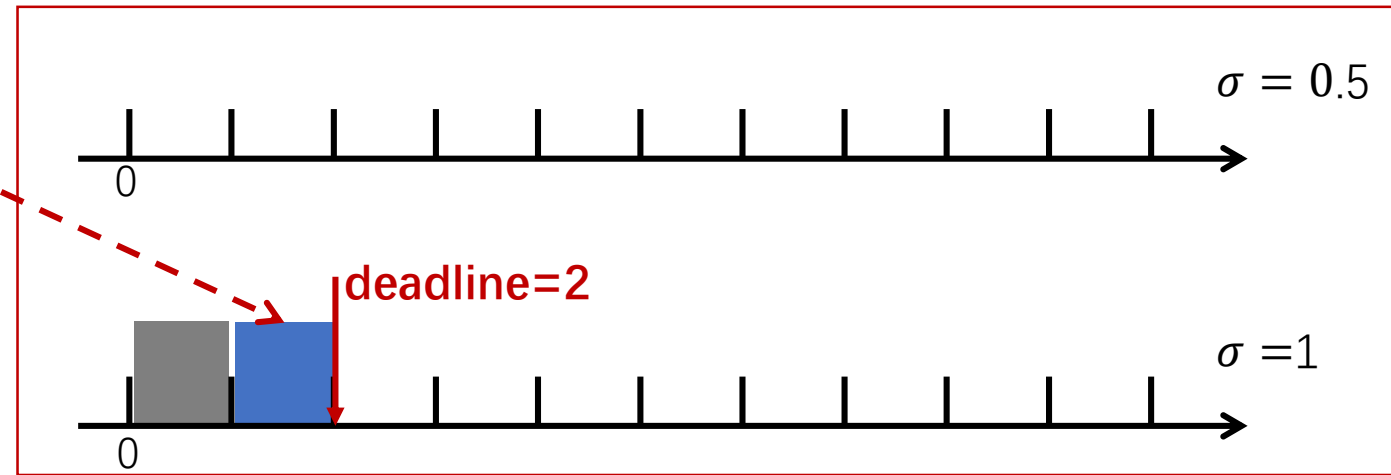
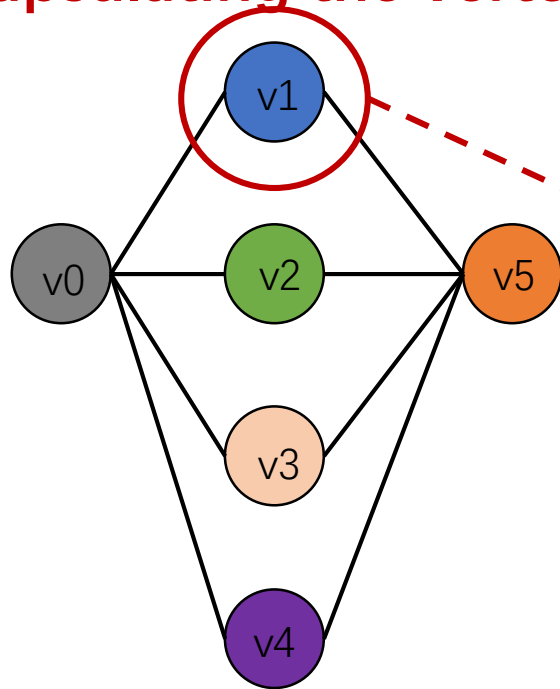


Runtime of a Mixed-Criticality Task

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- Mixed-Criticality tasks are encapsulated into mixed-criticality container-tasks

➤ **Encapsulating the vertex v1**

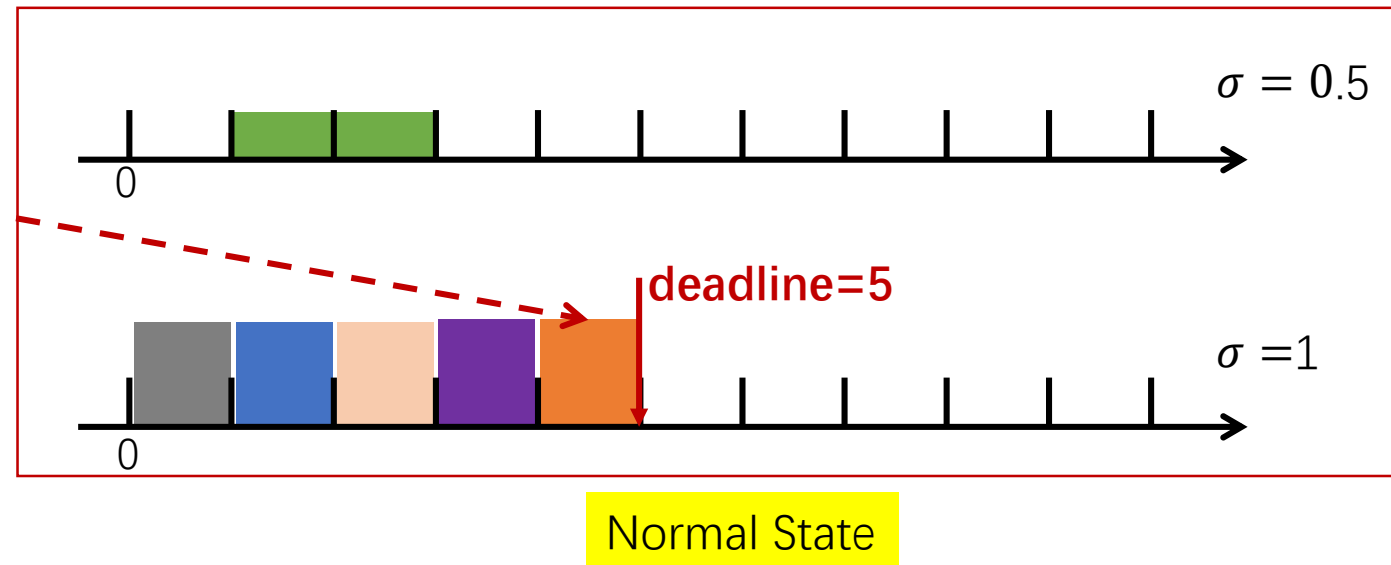
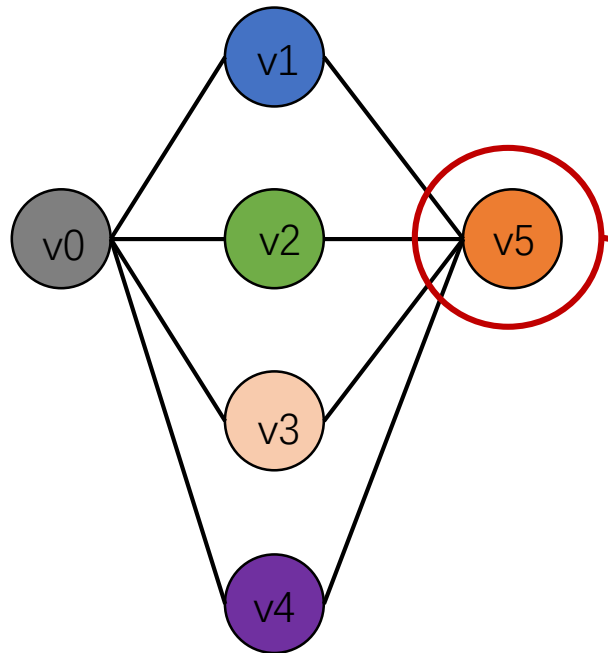


Normal State

Runtime of a Mixed-Criticality Task

$$\begin{aligned}c_{v0}^N = 1 \quad c_{v0}^O = 2, & \quad c_{v1}^N = 1 \quad c_{v1}^O = 3 \\c_{v2}^N = 1 \quad c_{v2}^O = 3, & \quad c_{v3}^N = 1 \quad c_{v3}^O = 3 \\c_{v4}^N = 1 \quad c_{v4}^O = 3, & \quad c_{v5}^N = 1 \quad c_{v5}^O = 2\end{aligned}$$

- Mixed-Criticality tasks are encapsulated into mixed-criticality container-tasks
 - Encapsulating the vertex $v5$

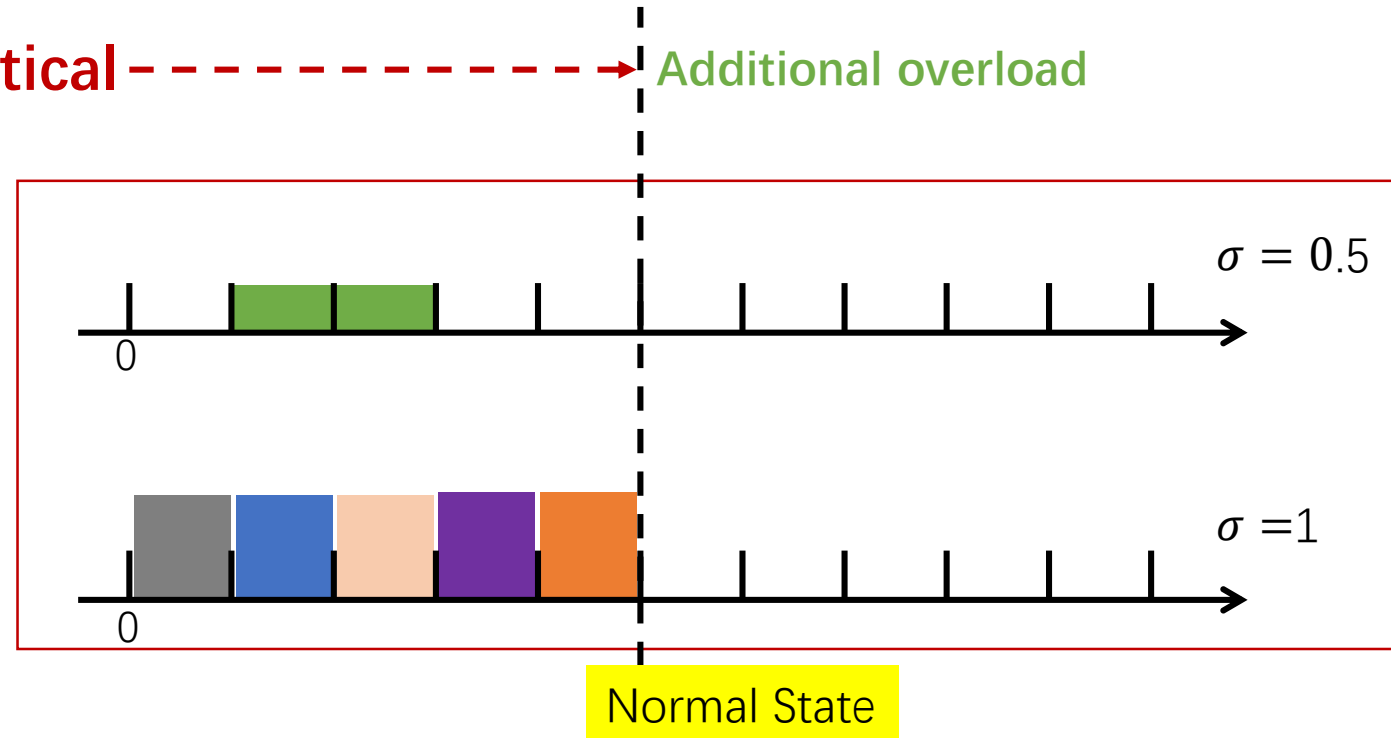


Runtime of a Mixed-Criticality Task

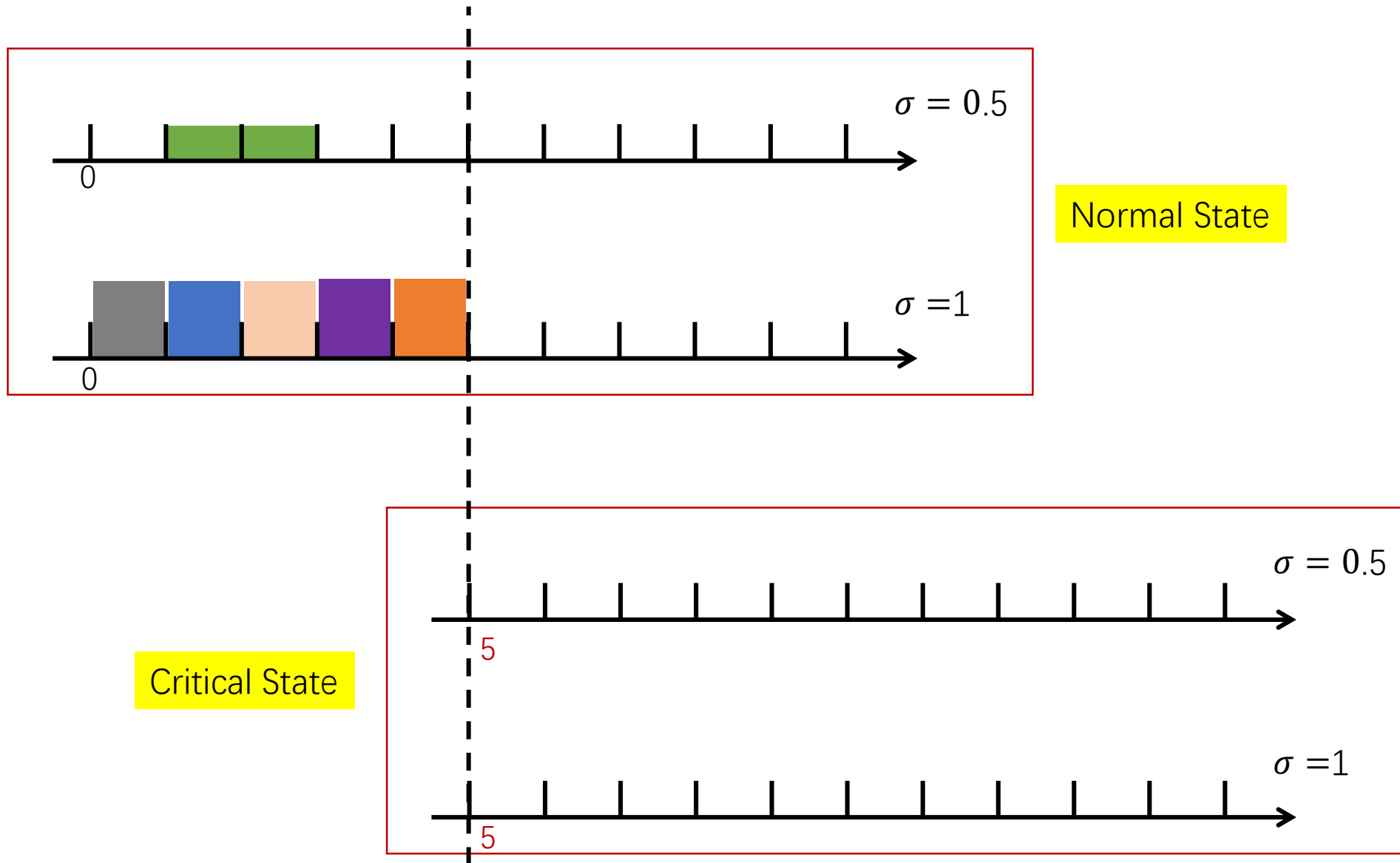
$$\begin{aligned}c_{v0}^N = 1 \quad c_{v0}^O = 2, & \quad c_{v1}^N = 1 \quad c_{v1}^O = 3 \\c_{v2}^N = 1 \quad c_{v2}^O = 3, & \quad c_{v3}^N = 1 \quad c_{v3}^O = 3 \\c_{v4}^N = 1 \quad c_{v4}^O = 3, & \quad c_{v5}^N = 1 \quad c_{v5}^O = 2\end{aligned}$$

- Mixed-Criticality tasks are encapsulated into mixed-criticality container-tasks

➤ **State transition: normal -> critical** - - - - - ➔ **Additional overload**



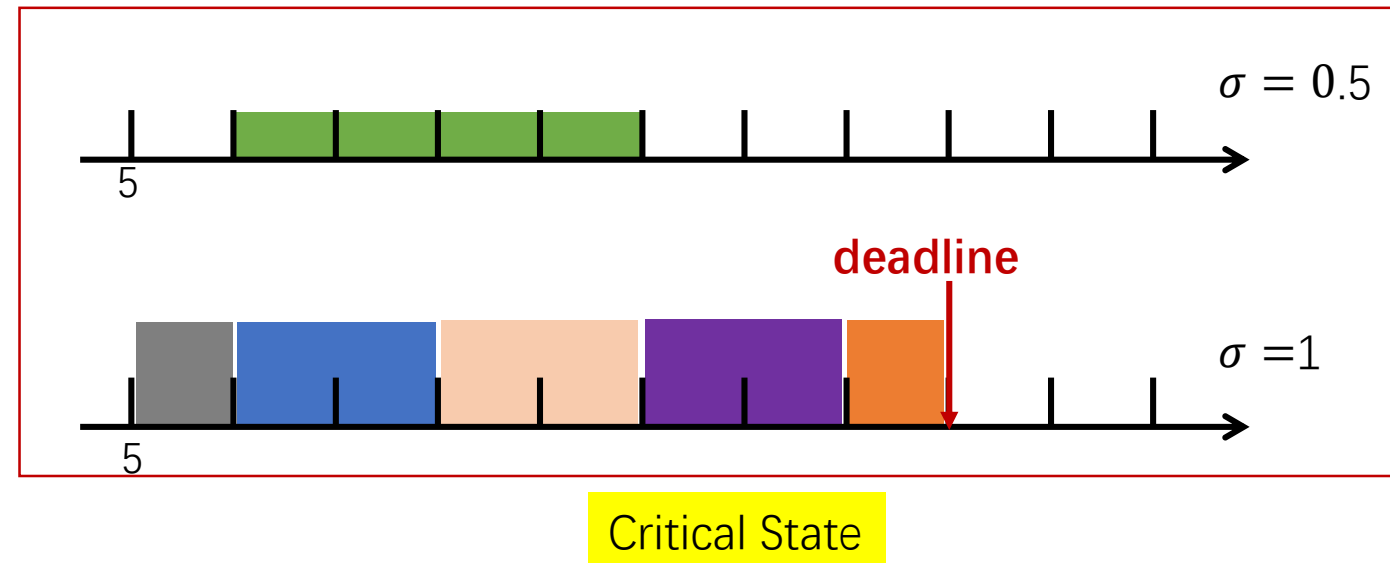
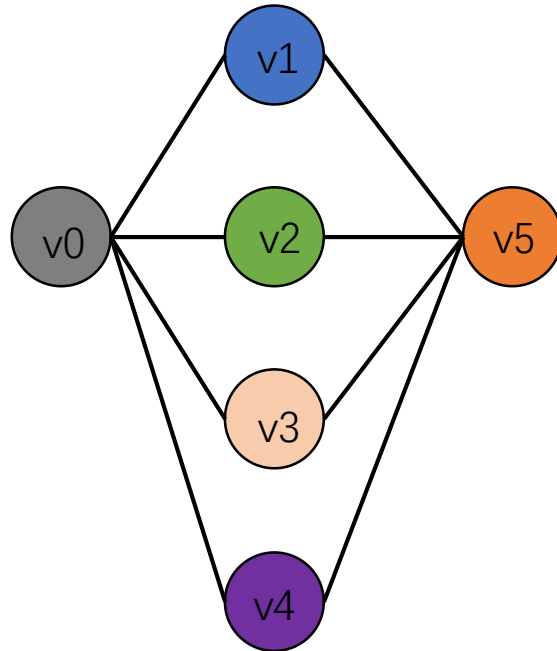
Runtime of a Mixed-Criticality Task



Runtime of a Mixed-Criticality Task

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- Mixed-Criticality tasks are encapsulated into mixed-criticality container-task
 - In critical states



Runtime of a Mixed-Criticality Task

- Mixed-Criticality tasks are encapsulated into mixed-criticality container-tasks
- Scheduling these mixed-criticality container-task to physical processor with a partitioned or global algorithm
 - First, system is in normal state and only normal mixed-criticality container-tasks are scheduled
 - When the system experiences state transition, all normal mixed-criticality container-tasks are banned from scheduling and only critical mixed-criticality container-tasks can run

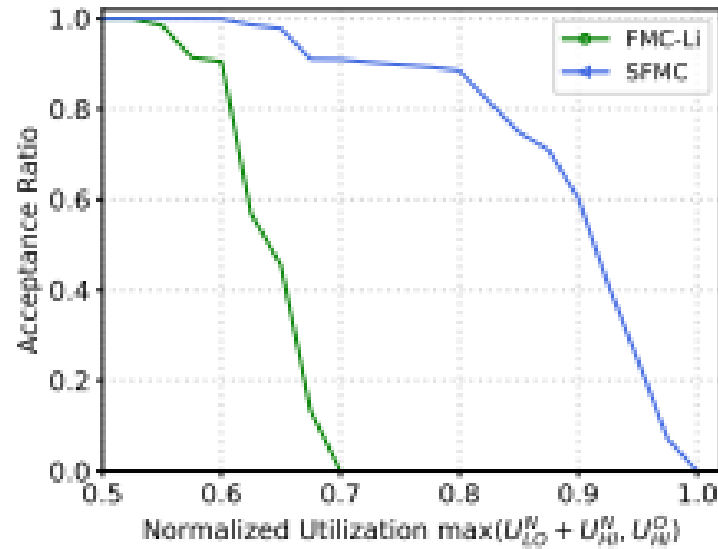
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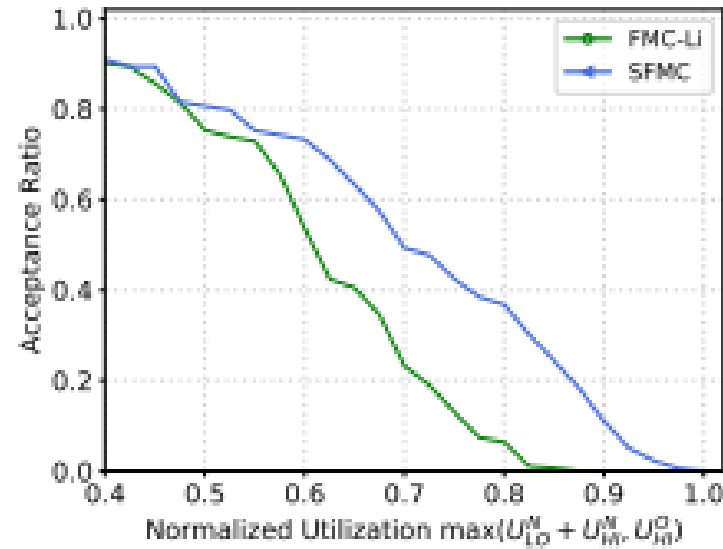
Evaluation

- Our task sets are generated based on OpenMP benchmarks and ompTG tool.
- Evaluate the acceptance ratio of task sets with different normalized utilizations.
- We compare our results with those in existing work for federated mixed-criticality scheduling.

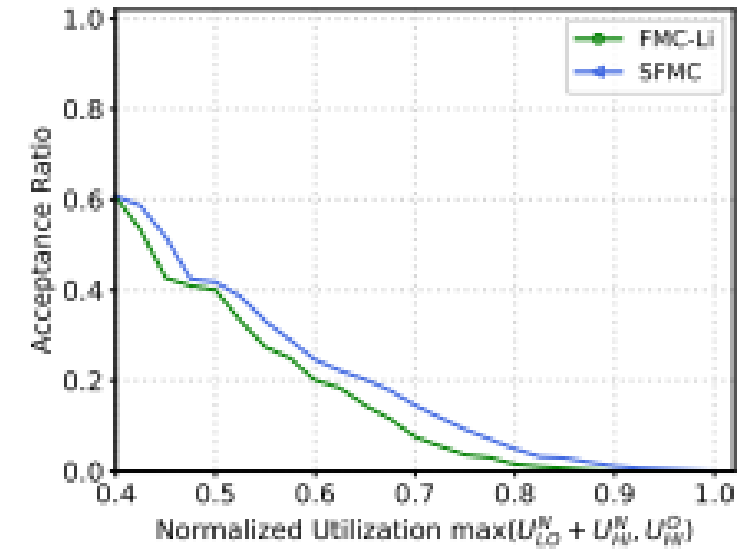
Evaluation



(a) $m=8$



(b) $m=16$



(c) $m=32$

Comparison of FMC-Li and SFMC

Semi-federated mixed-criticality algorithm has better schedulability performance

Thanks for your attention !